

# Bias Dependence of Non-Fourier Heat Conduction in GaN HEMTs

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# Overview

- ⚙ Self-heating in GaN HEMTs can cause reliability issues and degrade the device performance. Being the result of Joule heating, self-heating is highly **bias dependent**.
- ⚙ Previous studies on self-heating are mainly based on Fourier's law of heat conduction, **the non-Fourier effects have not been studied quantitatively**.
- ⚙ We reexamined the bias dependence of self-heating in GaN HEMTs by TCAD and phonon Monte Carlo simulations, and developed a **two-thermal-conductivity model** which can address the bias dependence of phonon ballistic effects easily.

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  - Phonon Ballistic Transport in GaN HEMTs
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# Thermal Issues in GaN HEMTs

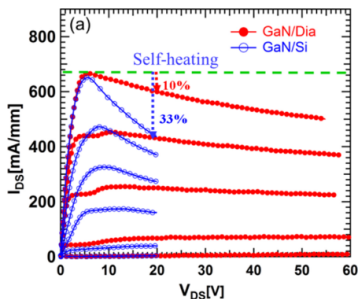


Figure 1:  $I_{DS} - V_{DS}$  of GaN/Dia and GaN/Si HEMTs <sup>1</sup>.

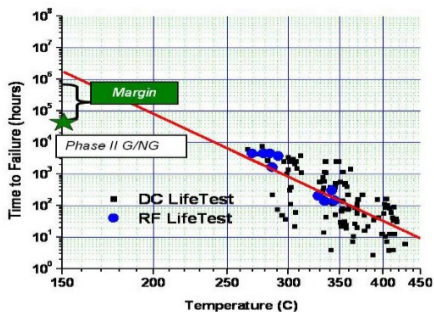


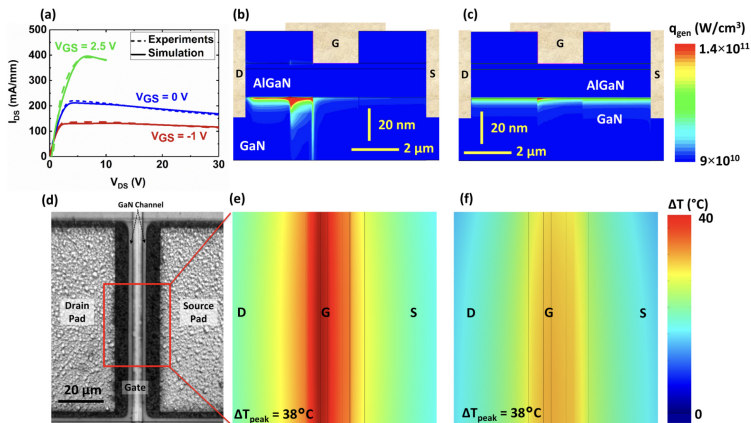
Figure 2: Mean time to failure (MTTF) for TriQuint GaN PAs <sup>2</sup>.

The significant overheating within the devices largely **degrades the electrical performance** and **shortens the device lifetime**.

<sup>1</sup>K. Ranjan, S. Arulkumar, G. Ng, *et al.*, "Investigation of self-heating effect on dc and rf performances in algan/gan hemts on cvd-diamond," *IEEE Journal of the Electron Devices Society*, vol. 7, pp. 1264–1269, 2019.

<sup>2</sup>M. Rosker, C. Bozada, H. Dietrich, *et al.*, "The darpa wide band gap semiconductors for rf applications (wbgs-rf) program: Phase ii results," *CS ManTech*, vol. 1, pp. 1–4, 2009.

# Bias Dependence of Self-Heating



**Figure 3:** Bias dependent results for channel conditions with  $V_{GS} = -1 \text{ V}$  and  $V_{GS} = 2.5 \text{ V}$ , respectively<sup>3</sup>,  $P_{diss} = 250 \text{ mW}$ .

<sup>3</sup>B. Chatterjee, C. Dundar, T. E. Beechem, *et al.*, "Nanoscale electro-thermal interactions in AlGaIn/GaN high electron mobility transistors," *Journal of Applied Physics*, vol. 127, no. 4, p. 044502, 2020.

# Bias Dependence of Self-Heating

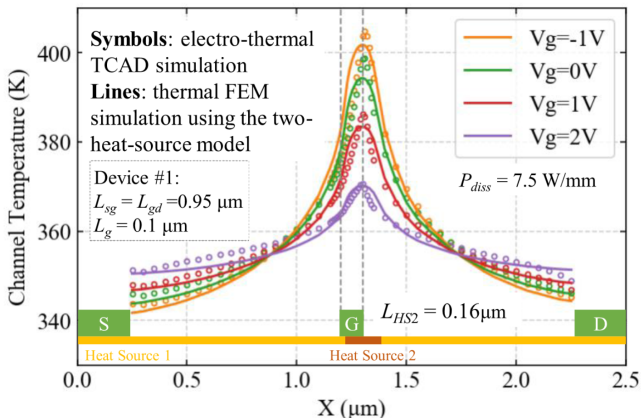


Figure 4: Temperature profiles across the channel at  $P_{diss} = 7.5 \text{ W/mm}$  and the four different biases<sup>4</sup>.

<sup>4</sup>X. Chen, S. Boumaiza, and L. Wei, "Modeling bias dependence of self-heating in gan hemts using two heat sources," *IEEE Transactions on Electron Devices*, vol. 67, no. 8, pp. 3082–3087, 2020.

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# Phonon Ballistic Transport

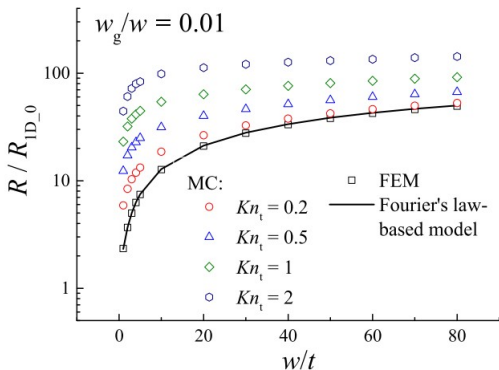


Figure 5: Dimensionless total thermal resistance as a function of  $w/t$ , with  $w_g/w = 0.005$  and  $0.01$ <sup>5</sup>.

Phonon Ballistic Transport can significantly increase the thermal resistance.

<sup>5</sup>Y.-C. Hua, H.-L. Li, and B.-Y. Cao, "Thermal spreading resistance in ballistic-diffusive regime for GaN HEMTs," *IEEE Transactions on Electron Devices*, vol. 66, no. 8, pp. 3296–3301, 2019.

The previous work considering the phonon transport in electrothermal simulations **did not give some general and clear conclusions** <sup>6–9</sup>.

Also, the bias dependence of phonon ballistic effects **has not been studied quantitatively**.

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<sup>6</sup>N. Donmez and S. Graham, "The impact of noncontinuum thermal transport on the temperature of algalan/gan hfets," *IEEE Transactions on Electron Devices*, vol. 61, no. 6, pp. 2041–2048, 2014.

<sup>7</sup>Q. Hao, H. Zhao, and Y. Xiao, "A hybrid simulation technique for electrothermal studies of two-dimensional GaN-on-SiC high electron mobility transistors," *Journal of Applied Physics*, vol. 121, no. 20, p. 204 501, 2017.

<sup>8</sup>Q. Hao, H. Zhao, Y. Xiao, *et al.*, "Hybrid electrothermal simulation of a 3-d fin-shaped field-effect transistor based on GaN nanowires," *IEEE Transactions on Electron Devices*, vol. 65, no. 3, pp. 921–927, 2018.

<sup>9</sup>B. Chatterjee, C. Dundar, T. E. Beechem, *et al.*, "Nanoscale electro-thermal interactions in AlGaN/GaN high electron mobility transistors," *Journal of Applied Physics*, vol. 127, no. 4, p. 044 502, 2020.

<sup>10</sup>H. Rezgui, F. Nasri, G. Nastasi, *et al.*, "Design optimization of nanoscale electrothermal transport in 10 nm soi finfet technology node," *Journal of Physics D: Applied Physics*, vol. 53, no. 49, p. 495 103, 2020.

# This Work

## Motivation

- 🔗 Reexamine the bias dependence of self-heating in GaN HEMTs with the consideration of phonon ballistic transport.

## This Work

- 🐧 **TCAD and Monte Carlo simulations** were conducted to study the self-heating in GaN HEMTs. Based on the **two-heat-source model**, this work proposed a **two-thermal-conductivity model** to consider the bias dependence of phonon ballistic effects easily.

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# Device Structure<sup>11</sup>

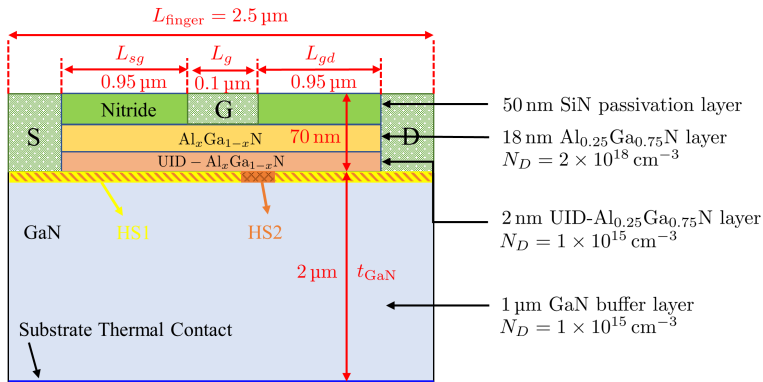


Figure 6: Schematic of the GaN HEMT for TCAD simulations.

<sup>11</sup>X. Chen, S. Boumaiza, and L. Wei, "Self-heating and equivalent channel temperature in short gate length gan hems," *IEEE transactions on electron devices*, vol. 66, no. 9, pp. 3748–3755, 2019.

# Output Characteristics

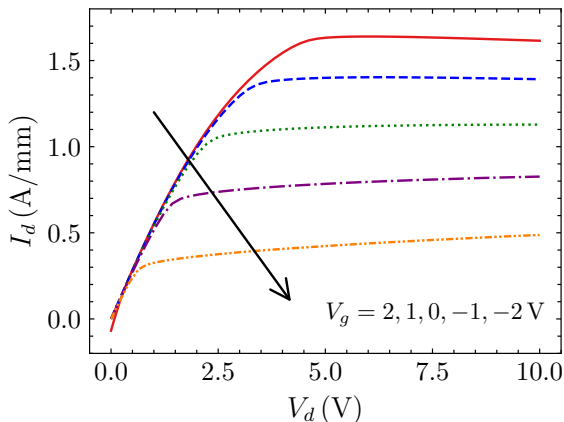


Figure 7: Output characteristics of the HEMT under  $V_g$  from  $-2$  V to  $2$  V with an interval of  $1$  V.

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# Phonon Monte Carlo Simulation

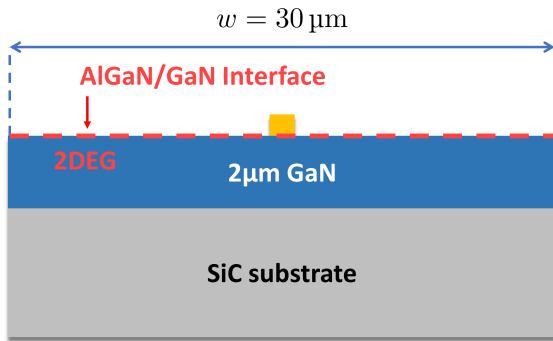


Figure 8: Schematic of GaN on SiC device for MC simulations.

# Phonon Dispersion

- An isotropic sine-shaped phonon dispersion (Born-von Karman dispersion) is used.
- Longitudinal and transverse branches are not differentiated.

$$\omega(k) = \omega_m \sin(\pi k / 2k_m)$$

$$k_m = \left( \frac{6\pi^2 N}{V} \right)^{1/3}, \quad a = \pi / k_m, \quad \omega_m = 2v_{0g} / a$$

# Relaxation time

Matthiessen's rule<sup>12</sup>:

$$\tau^{-1} = \tau_I^{-1} + \tau_U^{-1} = A\omega^4 + B\omega^2 T \exp(-C/T)$$

Thermal conductivity fitting:

$$\mathcal{L}(A, B, C) = \sum_T \left\| \frac{1}{3} \sum_{\rho} \int_0^{\omega_m} C_{\omega} v_{\omega} l_{\omega} d\omega - k_{\text{exp}} \right\|^2$$

$$C(\omega, \rho) = \hbar\omega D(\omega, \rho) \frac{\partial f^m}{\partial T} = \hbar\omega \frac{\kappa^2}{2\pi^2 |v_g|} \frac{\hbar\omega e^{\frac{\hbar\omega}{Tk_B}}}{T^2 k_B \left( e^{\frac{\hbar\omega}{Tk_B}} - 1 \right)^2}$$

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<sup>12</sup>G. Chen, *Nanoscale energy transport and conversion: a parallel treatment of electrons, molecules, phonons, and photons*. Oxford university press, 2005.

# Phonon Dispersion and Relaxation time

Table 1: Fitted phonon dispersion and scattering parameters<sup>13</sup>.

Parameter (Unit)	GaN	SiC
$k_0 (1 \times 10^9 \text{ m}^{-1})$	10.94	8.94
$\omega_m (1 \times 10^{13} \text{ rad/s})$	3.50	7.12
$a_D (\text{\AA})$	2.87	3.51
$A (1 \times 10^{-45} \text{ s}^3)$	5.26	1.00
$B (1 \times 10^{-19} \text{ s/K})$	1.10	0.596
$C (\text{K})$	200	235.0

<sup>13</sup>Q. Hao, H. Zhao, and Y. Xiao, "A hybrid simulation technique for electrothermal studies of two-dimensional GaN-on-SiC high electron mobility transistors," *Journal of Applied Physics*, vol. 121, no. 20, p. 204 501, 2017.

# Phonon Dispersion and Relaxation time

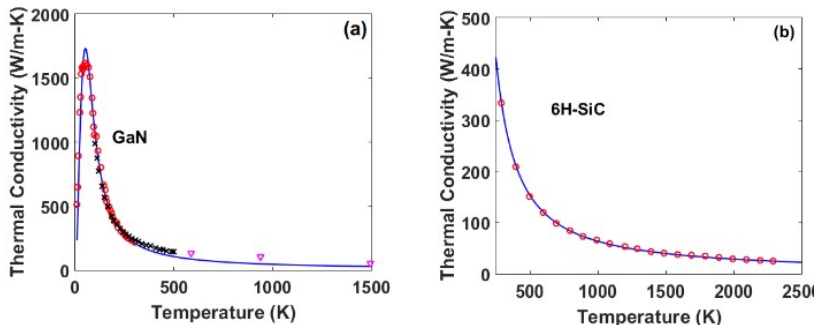


Figure 9: Thermal conductivity from model calculations (line), and from experiments (symbols)<sup>14</sup>.

<sup>14</sup>Q. Hao, H. Zhao, and Y. Xiao, "Multi-length scale thermal simulations of gan-on-sichigh electron mobility transistors," in *Multiscale Thermal Transport in Energy Systems*, Nova Science Publishers, 2016.

# Interface Phonon Transport

Based on **diffuse mismatch model (DMM)**, phonons are diffusively transmitted or reflected by an interface.

The frequency-dependent phonon transmissivity from material 1 to 2 is given as

$$T_{12}(\omega) = \frac{\sum_p v_{2,g,p}(\omega) D_{2,p}(\omega)}{\sum_p v_{1,g,p}(\omega) D_{1,p}(\omega) + \sum_p v_{2,g,p}(\omega) D_{2,p}(\omega)}$$

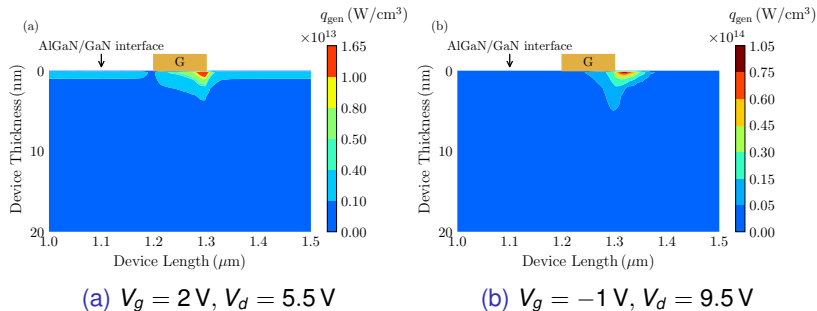
The thermal boundary resistance (TBR) of GaN/SiC calculated by MC is  $16 \text{ m}^2 \text{ K/GW}$ , which is in the same range of the experiments  $5 \text{ m}^2 \text{ K/GW}$ – $20 \text{ m}^2 \text{ K/GW}$ .

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# Bias-Dependent Heat Generation



**Figure 10:** The total power dissipation level for the two bias conditions,  $P = 7.5\text{ W/mm}$ .

# Two-Heat-Source Model

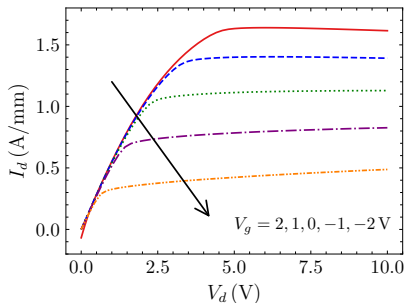
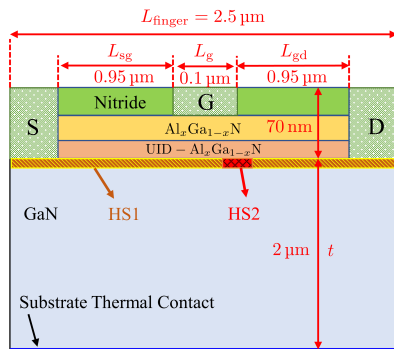


Figure 11: Schematic of the two-heat-source model.

$$\begin{cases} P_1 = I_d V_d, P_2 = 0, & V_d \leq V_{dsat} \\ P_1 = I_d V_{dsat}, P_2 = I_d (V_d - V_{dsat}), & V_d > V_{dsat} \end{cases}$$

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# Temperature Distribution

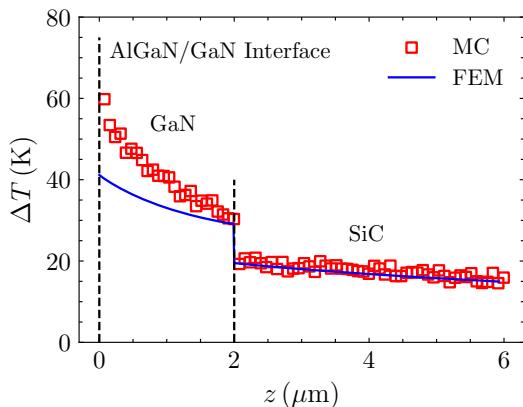
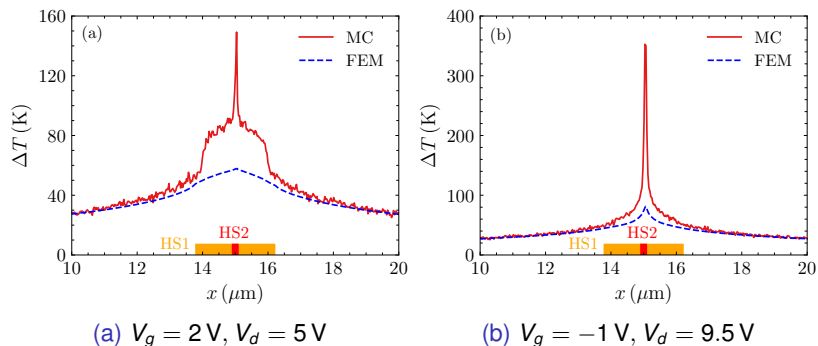


Figure 12: Temperature rise along the thickness direction at drain-side gate edge,  $V_g = 2\text{ V}$ ,  $V_d = 4\text{ V}$ .

Phonon ballistic effects mainly exist in GaN buffer layer.

# Bias-Dependent Channel Temperature



**Figure 13:** Temperature rise along the AlGaN/GaN interface,  $P_{\text{diss}} = 7.5\text{ W/mm}$ .

# Bias-Dependent Channel Temperature

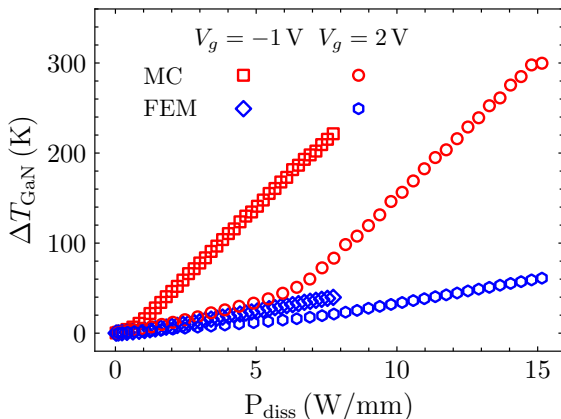


Figure 14: Maximum temperature rise in GaN layer at different biases predicted by MC and FEM.

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# Differential Thermal Resistance of GaN Layer

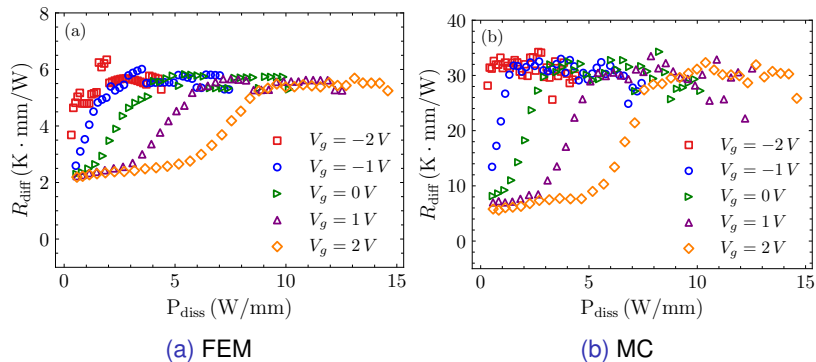
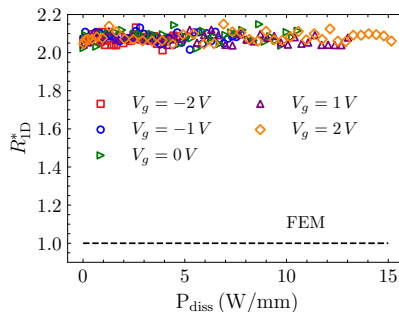


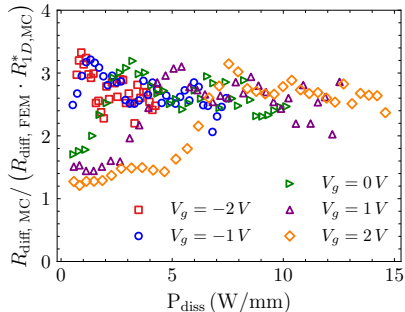
Figure 15: Differential thermal resistance  $R_{\text{diff}}$ , computed as the derivative of  $\Delta T_{\text{GaN}}$  versus  $P_{\text{diss}}$



# Thermal Resistance of GaN Layer



(a) 1D thermal resistance



(b) thermal resistance ratio

Figure 16: Thermal resistance of the GaN layer.

The cross-plane ballistic effect stays nearly constant at different biases, whereas the ballistic effect with the heat generation region size comparable with MFP is highly bias-dependent.

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# Effective Thermal Conductivity Model<sup>15,16</sup>

The degradation of the effective thermal conductivity is caused by the suppression of mean free paths of phonons,

$$k_{\text{eff}} = \frac{1}{3} \sum_j \int_0^{\omega_j} \hbar\omega \frac{\partial f_0}{\partial T} \text{DOS}_j(\omega) v_{g,\omega,j} l_{m,j} d\omega$$

Where

$$l_{m,j} = \frac{l_{0,j}}{\left(1 + \frac{2}{3} Kn_{t-\omega,j}\right) \left(1 + A_w \left(\frac{w_g}{w}, \frac{w}{t}\right) Kn_{w-\omega,j}\right) r_t r_{wg}}$$

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<sup>15</sup>Y.-C. Hua, H.-L. Li, and B.-Y. Cao, "Thermal spreading resistance in ballistic-diffusive regime for GaN HEMTs," *IEEE Transactions on Electron Devices*, vol. 66, no. 8, pp. 3296–3301, 2019.

<sup>16</sup>Y. Shen, Y.-C. Hua, H.-L. Li, *et al.*, "Spectral thermal spreading resistance of wide-bandgap semiconductors in ballistic-diffusive regime," *IEEE Transactions on Electron Devices*, vol. 69, no. 6, pp. 3047–3054, 2022.

# Two-Thermal-Conductivity Model

$$k_1 = 94.47 \text{ W/mK}, k_2 = 47.38 \text{ W/mK}$$

$$T_{max} = T_0 + \frac{k_{bulk}}{k_1} P_1 R_1 + \frac{k_{bulk}}{k_2} P_2 R_2$$

Where

$$\begin{cases} P_1 = I_d V_d, P_2 = 0, & V_d \leq V_{dsat} \\ P_1 = I_d V_{dsat}, P_2 = I_d (V_d - V_{dsat}), & V_d > V_{dsat} \end{cases}$$

$R_1$  and  $R_2$  are the thermal resistance seen by HS1 and HS2 of the GaN layer, respectively.  $T_0$  is the maximum temperature of bottom of the GaN layer predicted by FEM.

# Validation of the Model

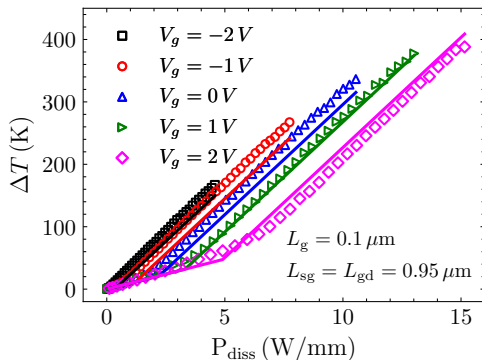


Figure 17: Maximum channel temperature rise versus total power dissipation  $P_{\text{diss}}$  at different biases.

# Devices with Different Geometries

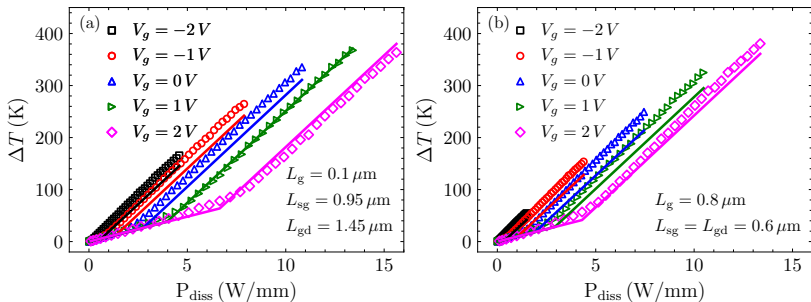


Figure 18: Maximum channel temperature rise versus total power dissipation  $P_{\text{diss}}$  at different biases.

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# Conclusion

- ⚙ Phonon ballistic effect can significantly **increase the thermal resistance of the GaN layer** and is highly bias-dependent.
- ⚙ The cross-plane ballistic effect stays nearly constant at different biases. Whereas with the concentration of heat generation, the ballistic effect with the heat generation size comparable with MFP increases significantly.
- ⚙ Based on the two-heat-source model, we proposed a two-thermal-conductivity model which provides a simple approach to incorporate the phonon ballistic effect with FEM **without the need for complicated multiscale electrothermal simulations.**



*Thank You!* 